

Maximum Expected Utility Why should we average utilities? Why not minimax? Principle of maximum expected utility: A rational agent should chose the action which maximizes its expected utility, given its knowledge Questions: Where do utilities come from? How do we know such utilities even exist? Why are we taking expectations of utilities (not, e.g. minimax)? What if our behavior can't be described by utilities?











Utility Scales

- Normalized utilities: u₊ = 1.0, u₋ = 0.0
- Micromorts: one-millionth chance of death, useful for paying to reduce product risks, etc.
- QALYs: quality-adjusted life years, useful for medical decisions involving substantial risk
- Note: behavior is invariant under positive linear transformation

$$U'(x) = k_1 U(x) + k_2$$
 where $k_1 > 0$

 With deterministic prizes only (no lottery choices), only ordinal utility can be determined, i.e., total order on prizes







Example: Human Rationality?
 Famous example of Allais (1953)
 A: [0.8,\$4k; 0.2,\$0] B: [1.0,\$3k; 0.0,\$0]
 C: [0.2,\$4k; 0.8,\$0] D: [0.25,\$3k; 0.75,\$0]
 Most people prefer B > A, C > D But if U(\$0) = 0, then B > A ⇒ U(\$3k) > 0.8 U(\$4k) C > D ⇒ 0.8 U(\$4k) > U(\$3k)